

Lines in the Coordinate Plane

Lesson Objective

FIND AND USE SLOPES OF LINES TO DETERMINE IF LINES ARE \parallel OR \perp ;
GRAPH LINES.

Algebra 1 Review

In Algebra 1, you learned how to find the slope of a line in the coordinate plane.

Slope: The slope of a line is a number that describes the STEEPNESS of the line.

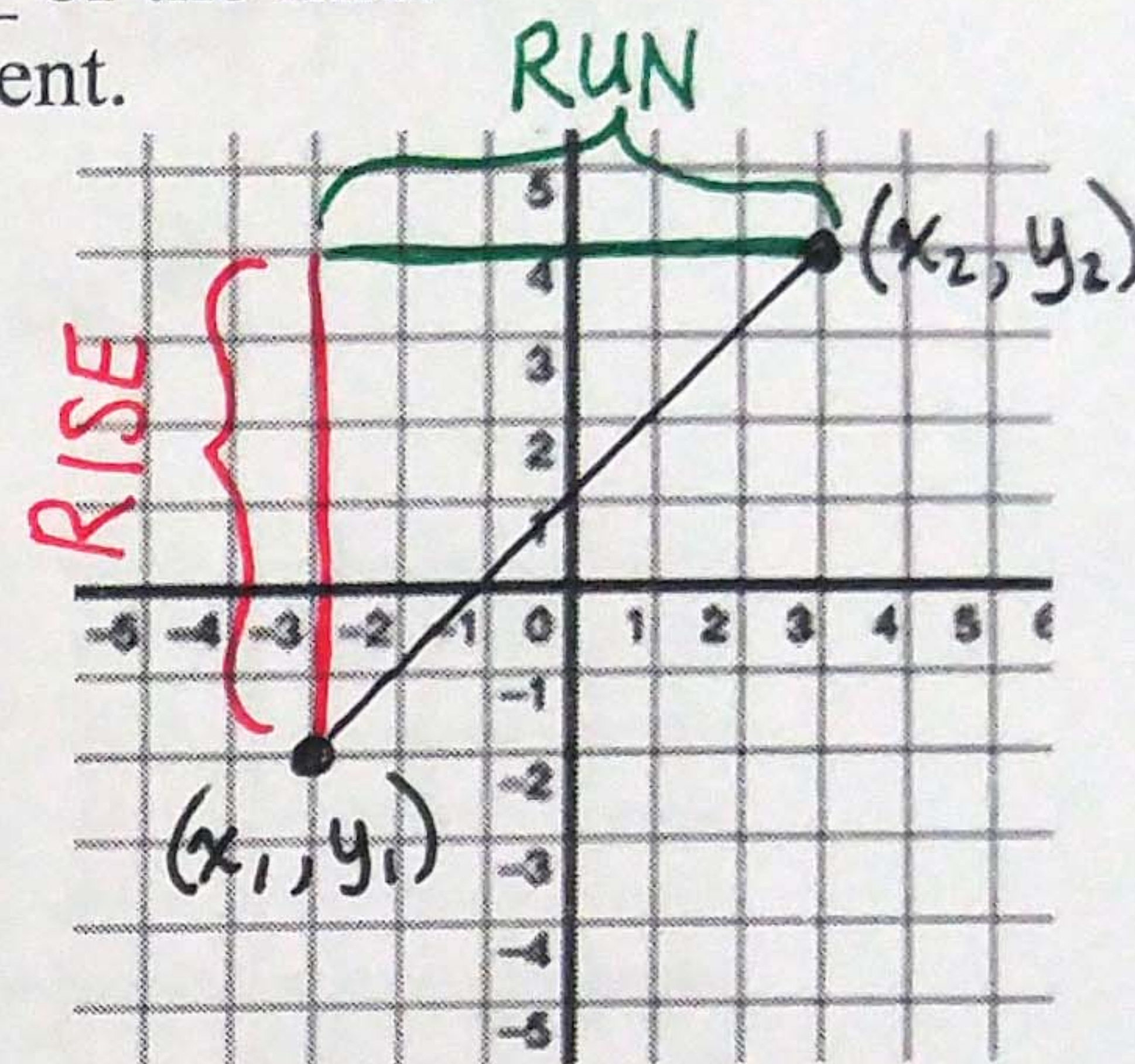
→ ANY two points can be used to determine the slope of a line or line segment.

The RISE is the difference in the y-values

The RUN is the difference in the x-values

The SLOPE is the RATIO of the RISE to the RUN.

$$m = \frac{\text{RISE}}{\text{RUN}} = \frac{y_2 - y_1}{x_2 - x_1}$$



Examples:

1. Use the slope formula to determine the slope of \overline{GH} if $G(2, 3)$ and $H(7, 5)$.
 $x_1 \ y_1 \quad x_2 \ y_2$

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{5 - 3}{7 - 2} = \frac{2}{5}$$

Summary: Slope of a Line

Positive Slope	Negative Slope	Zero Slope	Undefined Slope

More Algebra 1 Review

In Algebra 1, you learned how to graph lines in the coordinate plane using these formulas:

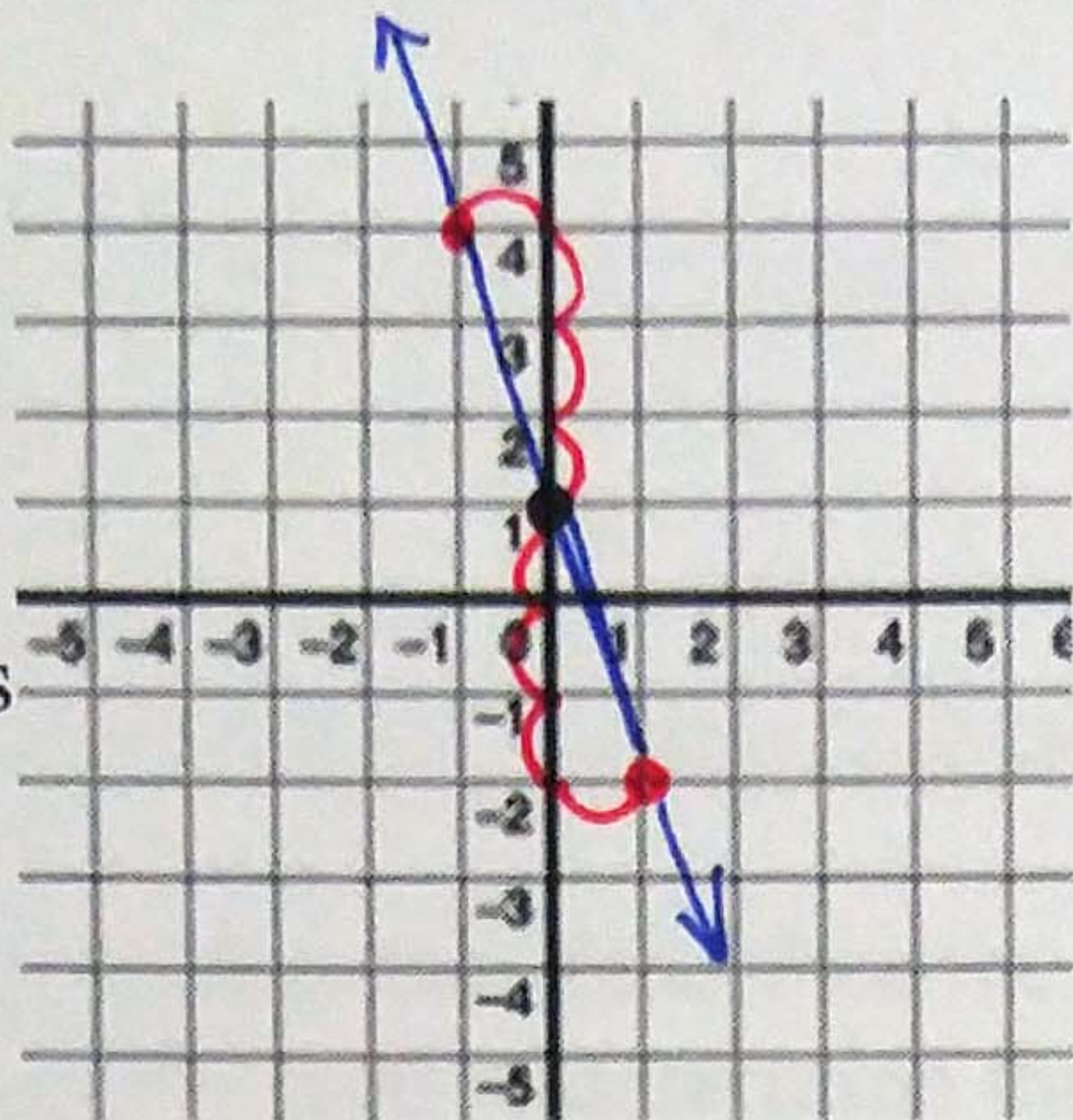
#1	Slope-Intercept Form	$y = mx + b$	m is the slope b is the y-intercept
#2	Point-Slope Form	$y - y_1 = m(x - x_1)$	m is the slope (x_1, y_1) is a point on the line

Graphing #1: Slope-Intercept Form

$$2. y = -3x + 1$$

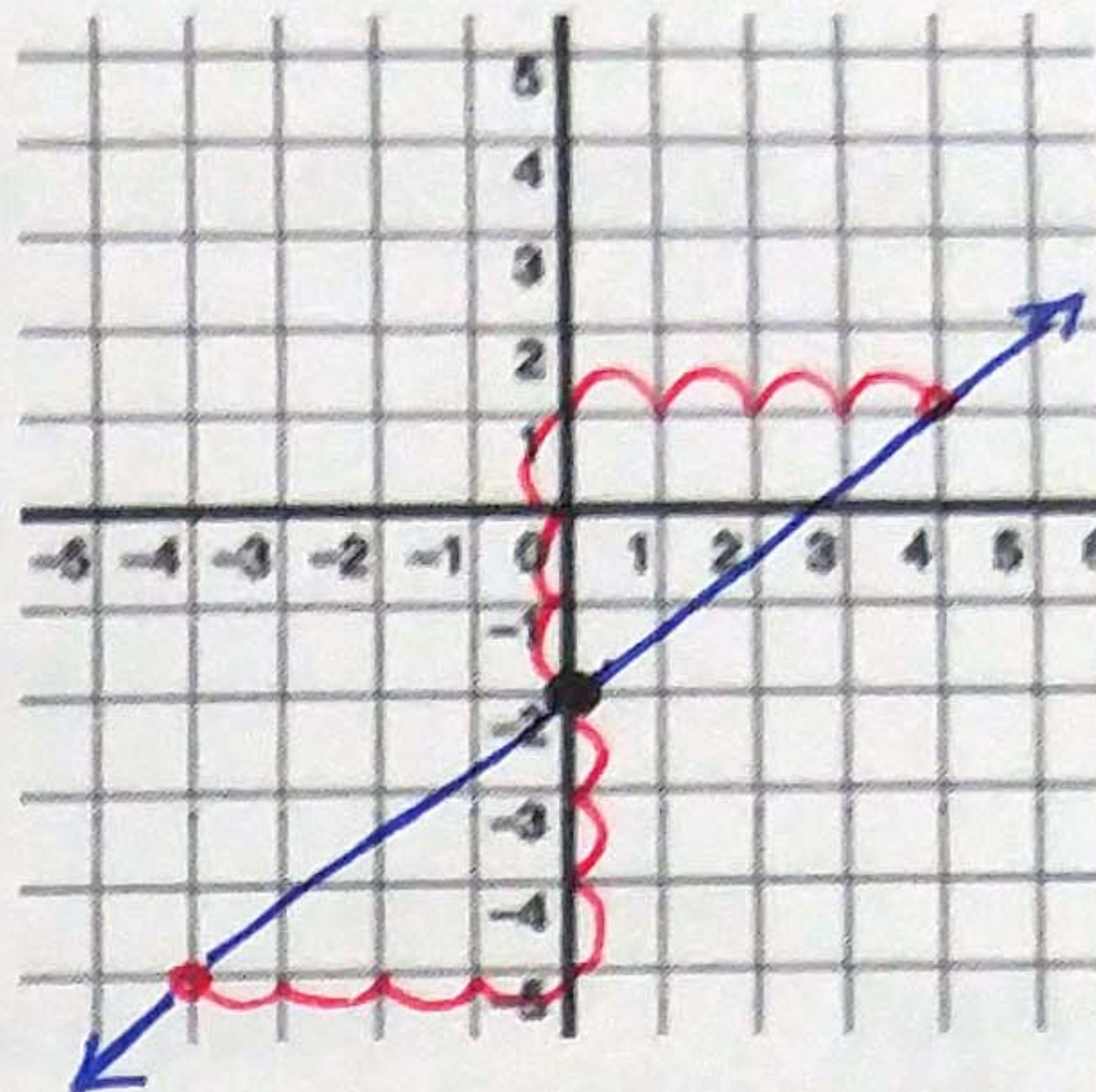
$m = -3 = \frac{-3}{1}$ OR $\frac{3}{-1}$
 $b = 1$

- (1) Graph the y-int (b)
- (2) From the y-int, plot new points using the slope (m) "rise/run"
- (3) Make at least 3 points
- (4) Connect the points with a straightedge



$$3. y = \frac{3}{4}x - 2$$

$m = \frac{3}{4}$ OR $\frac{-3}{-4}$
 $b = -2$

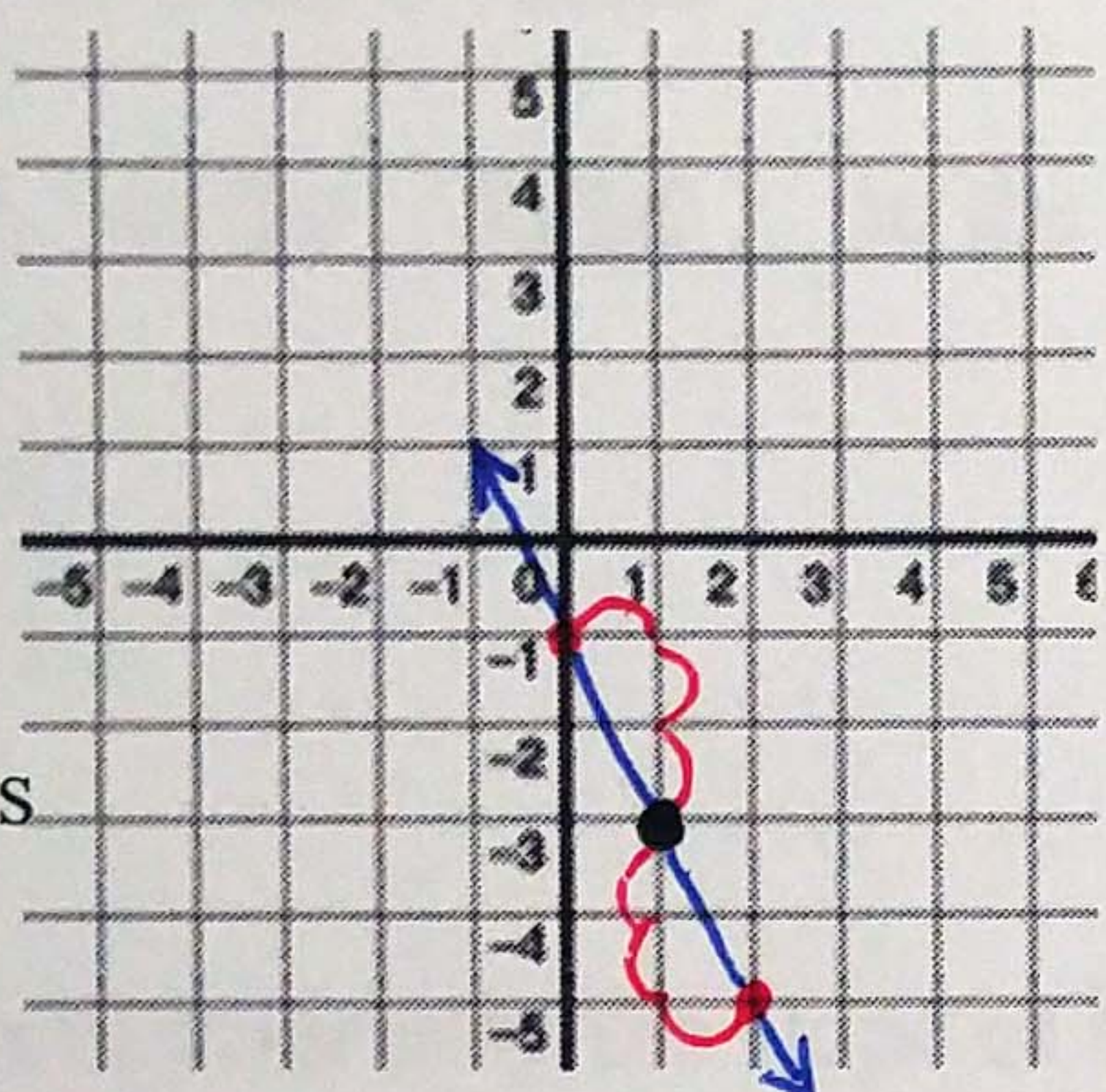


Graphing #2: Point-Slope Form

$$4. y + 3 = -2(x - 1)$$

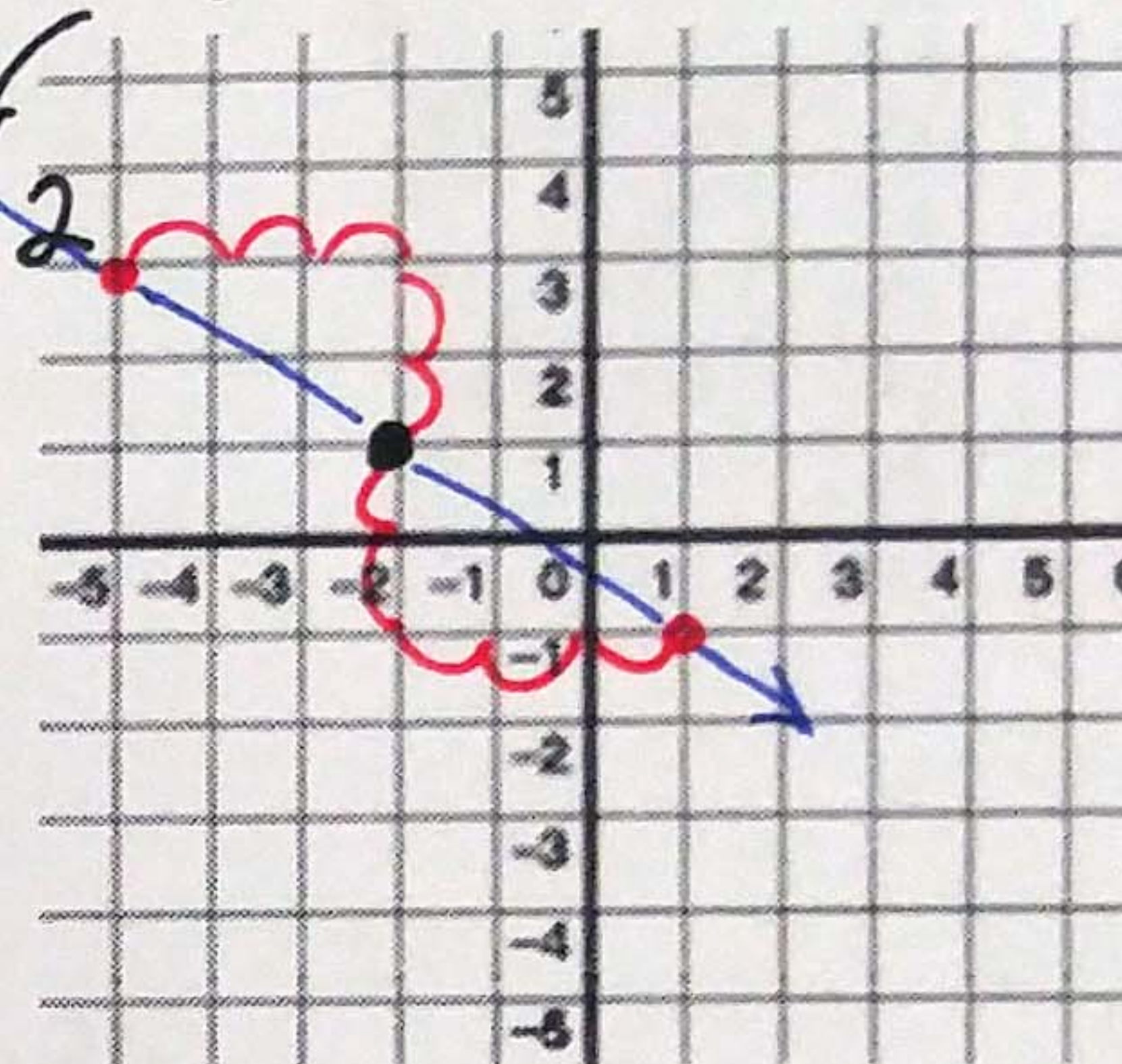
$m = -2 = \frac{-2}{1}$ OR $\frac{2}{-1}$
 $y_1 = 3$ $x_1 = 1$

- (1) Graph the point (x_1, y_1)
- (2) From this point, plot new points using the slope (m) "rise/run"
- (3) Make at least 3 points
- (4) Connect the points with a straightedge



$$5. y - 1 = -\frac{2}{3}(x + 2)$$

$m = -\frac{2}{3}$ OR $\frac{2}{-3}$
 $y_1 = 1$ $x_1 = -2$



Vertical Lines	The equation of a vertical line is $x = h$, where h is the x -intercept.	Example: $x = 5$	
Horizontal Lines	The equation of a horizontal line is $y = k$, where k is the y -intercept.	Example: $y = -3$	

Connecting it to Geometry

Parallel Lines Theorem (\parallel Lines Thm)	In a coordinate plane, two distinct non-vertical lines are parallel if and only if they have the <u>SAME</u> slope. Also, any two vertical lines are parallel.
Perpendicular Lines Theorem (\perp Lines Thm)	In a coordinate plane, two distinct non-vertical lines are perpendicular if and only if the <u>PRODUCT</u> of their slopes is <u>-1</u> . *PRODUCT = MULTIPLY Also, horizontal lines are perpendicular to vertical lines.

Example:

"NEGATIVE RECIPROALS" i.e. $\frac{2}{3}$ AND $-\frac{3}{2}$

6. Determine which of the lines are parallel and which of the lines are perpendicular.

$$m_{(a)} = \frac{3-2}{0-(-3)} = \frac{1}{3}$$

$$m_{(d)} = \frac{2-0}{-3-(-2)} = \frac{2}{-1} = -2$$

$$m_{(b)} = \frac{0-(-1)}{2-0} = \frac{1}{2}$$

$$m_{(c)} = \frac{-4-(-5)}{1-(-1)} = \frac{1}{2}$$

$b \parallel c$: SAME SLOPE

$b \perp d$ AND : $(\frac{1}{2})(-2) = -1$
 $c \perp d$

