

Measuring Angles

Lesson Objective

INBAT find measures of and classify different types of angles.

Naming Angles

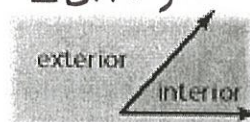
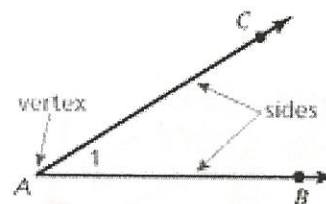
Angle: An angle is a set of points consisting of 2 diff. rays that have the same endpoint called the vertex.

→ The rays are the sides of the angle.

Name: ① use vertex ($\angle A$)

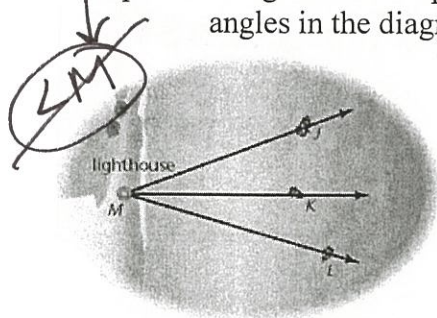
② use points on rays + vertex ($\angle CAB$ or $\angle BAC$)

③ use # inside the angle ($\angle 1$)



***If more than one angle has the same vertex, the name $\angle(\text{vertex point})$ cannot be used!!!

Example: 1. A lighthouse keeper measures the angles formed by the lighthouse at point M and 3 boats. Name 3 angles in the diagram.



$\angle JMK$ (or $\angle KMJ$)

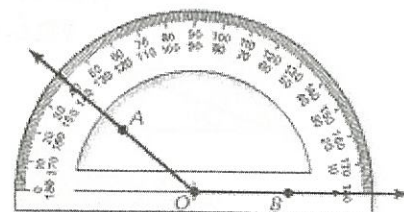
$\angle KML$ (or $\angle LMK$)

$\angle JML$ (or $\angle LMJ$)

Measuring Angles

Protractor Postulate: The measure of $\angle AOB$ ($m\angle AOB$) is equal to the difference between the real numbers matched with \overrightarrow{OA} and \overrightarrow{OB} .

$$m\angle AOB = |40 - 180| = |-140| = 140^\circ$$



Classifying Angles

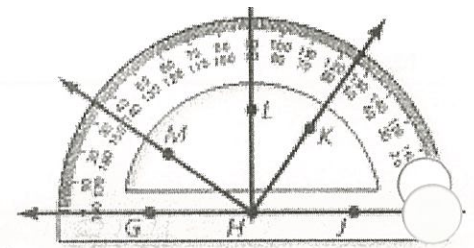
Acute Angle	Right Angle	Obtuse Angle	Straight Angle
$0^\circ < \text{angle} < 90^\circ$	$= 90^\circ$	$90^\circ < \text{angle} < 180^\circ$	$= 180^\circ$

Example: 2. Find the measure of each angle. Then classify each angle.

a. $\angle GHK$

b. $\angle JHL$

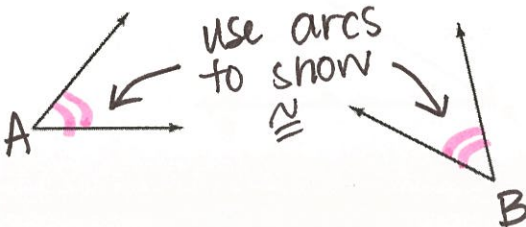
c. $\angle LHK$



Identifying Congruent Angles

Congruent Angles: Two angles are congruent when they have the same degree measure.

MEASURES of angles are EQUAL



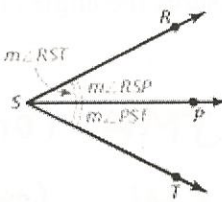
$$m\angle A = m\angle B$$

$$\angle A = \angle B$$

$$\angle A \cong \angle B$$

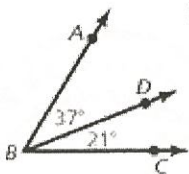
$$m\angle A \cong m\angle B$$

Angle Addition Postulate

Words	Symbols
If P is in the <u>inside</u> of $\angle RST$, then the measure of $\angle RST$ is equal to the <u>sum</u> of the measures of <u>$\angle RSP$</u> and <u>$\angle PST$</u> .	If P is in the <u>inside</u> of $\angle RST$, then  $m\angle RST = m\angle RSP + m\angle PST$

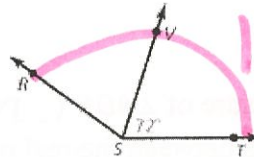
Example:

3. Find $m\angle ABC$.



$$\begin{aligned} m\angle ABC &= m\angle ABD + m\angle DBC \\ m\angle ABC &= 37^\circ + 21^\circ \\ &= \boxed{58^\circ} \end{aligned}$$

4. $m\angle RST = 114^\circ$. Find $m\angle RSV$.

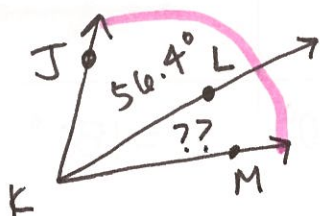


$$m\angle RST = m\angle RSV + m\angle VST$$

$$114 = m\angle RSV + 72$$

$$\boxed{42^\circ = m\angle RSV}$$

5. L is in the interior of $\angle JKM$. Find $m\angle LKM$ if $m\angle JKL = 56.4^\circ$ and $m\angle JKM = 82.5^\circ$. Sketch a diagram first.



$$\begin{aligned} m\angle JKM &= m\angle JKL + m\angle LKM \\ 82.5^\circ &= 56.4^\circ + m\angle LKM \\ -56.4 \quad -56.4 \\ \hline \boxed{26.1^\circ} &= m\angle LKM \end{aligned}$$